

GEOMETRY OF JETS AND FIELDS

10-16 MAY 2015, BĘDLEWO, POLAND

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WARSAW CENTER OF MATHEMATICS
AND COMPUTER SCIENCE

INVITED SPEAKERS

- Jose-Fernando Carinena (University of Zaragoza)
- Janusz Grabowski (Polish Academy of Sciences)
- Partha Guha (S. N. Bose National Centre for Basic Sciences)
- Simone Gutt (Universite Libre de Bruxelles)
- Alberto Ibort (Universidad Carlos III de Madrid)
- Madeleine Jotz Lean (University of Sheffield)
- Jerzy Kijowski (Centre of Theoretical Physics Polish Academy of Sciences)
- Yvette Kossmann-Schwarzbach (Ecole Polytechnique)
- Manuel de Leon (Instituto de Ciencias Matematicas)
- Charles-Michel Marle (Universite Pierre et Marie Curie)
- Giuseppe Marmo (Universita di Napoli "Federico II")
- Juan-Carlos Marrero (Universidad de La Laguna)
- Eduardo Martinez (Memorial University of Newfoundland)
- Guowu Meng (Hong Kong University of Science and Technology)
- Norbert Poncin (University of Luxemburg)
- Olga Rossi (The University of Ostrava)
- Gennadi Sardanashvily (Moscow State University)
- Yunhe Sheng (School of Mathematics Jilin University)
- Alexandre Vinogradov (Levi-Civita Institute)
- Luca Vitagliano (University of Salerno)
- Aissa Wade (Penn State University)
- Ping Xu (Penn State University)

AIM AND SCOPE

The main topics of the conference are:

- Geometry of multivector and jet bundles.
- Covariant formulation of field theories.
- Infinite order theories: geometry, symmetries, and reductions.
- Variational calculus.
- Supergeometric and cohomological methods in PDEs and field quantization.

SCHEDULE

	11 th May	12 th May	13 th May	14 th May	15 th May
09.00-10.00	Ch. M. Marle	S. Gutt	A. Vinogradov	G. Sardanashvily	L. Vitagliano
10.00-11.00	Y. Kosmann-Schwarzbach	A. Wade	O. Rossi	M. de Leon	P. Guha
11.00-11.30	COFFEE	COFFEE	COFFEE	COFFEE	COFFEE
11.30-12.30	J. Grabowski	N. Poncin	J.F. Carinena	A. Ibort	E. Martinez
13.00-14.00	LUNCH	LUNCH	LUNCH	LUNCH	LUNCH
14.00-15.00	BREAK	BREAK	TRIP	BREAK	BREAK
15.00-16.00	G. Marmo	M. Jotz Lean		G. Meng	P. Xu
16.00-16.30	COFFEE	COFFEE		COFFEE	COFFEE
16.30-17.00	J. Kijowski	Y. Sheng		J.C. Marrero	A. Sergyeyew E. Vishnyakova
17.30-18.30		poster session		poster session	C. Vizman best poster
19.00	GRILL	DINER	BANQUET	DINER	DINER

MJ: Accomodation, meals, registration, busses

MJ: conference events: banquet trip

MJ: Practical information: Wifi, visit Poznań, web page, contact to the organizers

SCIENTIFIC PROGRAM

Saturday-Sunday 9th – 10th May

all day arrivals, registration

Monday 11th May

09.00-17.30 Session I, Chairman: XX

09.00-10.00 **Charles-Michel Marle:** *The works of William Rowan Hamilton in Geometric Optics and the Malus-Dupin theorem*

10.00-11.00 **Yvette Kosmann-Schwarzbach:** *Multiplicativity, from Lie groups to generalized geometry*

11.30-12.30 **Janusz Grabowski:** *New developments in geometric mechanics*

15.00-16.00 **Giuseppe Marmo:** *A quantum route to Hamilton-Jacobi theory*

16.30-17.30 **Jerzy Kijowski:** *TBA*

Tuesday 12th May

09.00-17.30 Session II, Chairman: XX

09.00-10.00 **Simone Gutt:** *Submanifolds in symplectic geometry and Radon transforms*

10.00-11.00 **Aissa Wade:** *On cosymplectic groupoids*

11.30-12.30 **Norbert Poncin:** *Multi-graded algebra and geometry*

15.00-16.00 **Madeleine Jotz Lean:** *TBA*

16.30-17.30 **Yunhe Sheng:** *Lie 2-algebras, homotopy Poisson manifolds and Courant algebroids*

17.30-18.30 poster session

Wednesday 13th May

09.00-12.30 Session III, Chairman: XX

09.00-10.00 **Alexandre Vinogradov:** *DCinCA, NPDEs and (Q)FT : some problems and perspectives*

10.00-11.00 **Olga Rossi:** *Geometry of PDEs and Hamiltonian systems*

11.30-12.30 **Jose-Fernando Carinena:** *Revisiting Lie integrability by quadratures from a geometric perspective*

Scientific program (continued)

Thursday 14 th May

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| 09.00-17.30 | Session IV, Chairman: XX |
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| 09.00-10.00 | Gennadi Sardanashvily: <i>Noether theorems in a general setting. Reducible graded Lagrangians</i> |
| 10.00-11.00 | Manuel de Leon: <i>Hamilton-Jacobi theory in Cauchy data space</i> |
| 11.30-12.30 | Alberto Ibort: <i>On the multisymplectic formalism of first-order Hamiltonian field theories on manifolds with boundary: an application to Palatini's gravity</i> |
| 15.00-16.00 | Guowu Meng: <i>Tulczyjew's approach for particles in gauge fields</i> |
| 16.30-17.30 | Juan-Carlos Marrero: <i>Hamilton-Poincaré field equations</i> |
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| 17.30-18.30 | poster session |

Friday 15 th May

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| 09.00-17.30 | Session V, Chairman: XX |
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| 09.00-10.00 | Luca Vitagliano: <i>Vector bundle valued differential forms on NQ-manifolds</i> |
| 10.00-11.00 | Partha Guha: <i>Inverse problem of calculus of variations and the last Jacobi multiplier</i> |
| 11.30-12.30 | Eduardo Martinez: <i>Jets and fields on Lie algebroids</i> |
| 15.00-16.00 | Ping Xu: <i>Infinite jets of exponential maps and L_∞-algebras</i> |
| 16.30-17.00 | Artur Sergyeyev: <i>A new class of (3+1)-dimensional integrable systems related to contact geometry</i> |
| 17.00-17.30 | Elizaveta Vishnyakova: <i>Flag supermanifolds: definition, properties and applications</i> |
| 17.30-18.00 | Cornelia Vizman: <i>TBA</i> |
| 18.00-18.30 | best poster talk |

PLENARY TALKS

Jose F. Cariñena (University of Zaragoza)

Revisiting Lie integrability by quadratures from a geometric perspective

Abstract: The classical result of Lie on integrability by quadratures will be reviewed and some generalizations will be proposed. After a short review of the classical Lie theorem, a finite dimensional Lie algebra of vector fields is considered and the most general conditions under which the integral curves of one of the fields can be obtained by quadratures in a prescribed way will be discussed, determining also the number of quadratures needed to integrate the system. The theory will be illustrated with examples and an extension of the theorem where the Lie algebras are replaced by some distributions will also be presented.

Janusz Grabowski (Polish Academy of Sciences)

New developments in geometric mechanics

Abstract: We introduce the concept of a graded bundle, generalizing that of a vector bundle, its linearization, and a double structure of this kind. Then, we present applications in classical field theories, including the Plateau problem, and mechanics with higher order Lagrangians.

Partha Guha (S. N. Bose National Centre for Basic Sciences)

Inverse problem of calculus of variations and the last Jacobi multiplier

Abstract: TBA

Simone Gutt (Universite Libre de Bruxelles)

Submanifolds in symplectic geometry and Radon transforms

Abstract: TBA

Alberto Ibort (Universidad Carlos III de Madrid)

On the multisymplectic formalism of first-order Hamiltonian field theories on manifolds with boundary: an application to Palatini's gravity

Abstract: The multisymplectic formalism for first-order field theories on manifolds with boundary is discussed. A theory of boundary conditions and a canonical formalism near the boundary are obtained. Palatini's gravity will be reviewed from this perspective.

Madeleine Jotz Lean (University of Sheffield)

Title: TBA

Abstract: TBA

Jerzy Kijowski (Centre of Theoretical Physics Polish Academy of Sciences)

Title: TBA

Abstract: TBA

Yvette Kosmann-Schwarzbach (Ecole Polytechnique)

Multiplicativity, from Lie groups to generalized geometry

Abstract: TBA

Manuel de León (Instituto de Ciencias Matematicas)

Hamilton-Jacobi theory in Cauchy data space

Abstract: We shall develop a Hamilton-Jacobi theory of Classical Field Theories using a multisymplectic setting, as well as the corresponding Hamilton-Jacobi theory in the Cauchy data space

Charles-Michel Marle (Universite Pierre et Marie Curie)

The works of William Rowan Hamilton in Geometric Optics and the Malus-Dupin theorem

Abstract: In this talk I will discuss the works of William Rowan Hamilton in Geometric Optics, with emphasis on the Malus-Dupin theorem. According to that theorem, a family of light rays depending on two parameters can be focused to a single point by an optical instrument made of reflexing or refracting surfaces if and only if, before entering the optical instrument, the family of rays is rectangular (*i.e.*, admits orthogonal surfaces). Moreover, that theorem states that a rectangular system of rays remains rectangular after an arbitrary number of reflexions through, or refractions across, smooth surfaces of arbitrary shape. I will present the original proof of that theorem due to Hamilton, along with another proof founded in symplectic geometry. It was the proof of that theorem which led Hamilton to introduce his *characteristic function* in Optics, then in Dynamics under the name *action integral*.

Giuseppe Marmo (Universita di Napoli “Federico II”)

A quantum route to Hamilton-Jacobi theory

Abstract: There is a wide spread belief that the appropriate description of the physical world should be quantum, therefore one should require that the classical description should be an appropriate limit of the quantum one. From this point of view it is quite

reasonable to ask about the fate of the complex structure and the linear structure available in the quantum setting but absent at the classical level. In this talk I shall discuss some of these questions, emerging when we go from the linear Schroedinger equation to the nonlinear Hamilton-Jacobi equation.

Juan-Carlos Marrero (Universidad de La Laguna)
Hamilton-Poincaré field equations

Abstract: In this talk, I will present several geometric descriptions of the Hamilton-Poincaré field equations for an equivariant hamiltonian section. First of all, I will discuss a local derivation of these equations. Next, I will present an intrinsic expression of the equations using the theory of prolongations of invariant vector fields to the reduced extended multimomentum bundle. A third description of the Hamilton-Poincaré field equations will be discussed using a principal connection (in the principal bundle with structural group, the symmetry group, and with total space, the configuration space of the theory). Finally, I will apply the previous results to some examples.

Eduardo Martínez (University of Zaragoza)
Jets and fields on Lie algebroids

Abstract: I will review on the extension of the concept of jet to the context of Lie algebroids and its application in Classical Field Theory.

Guowu Meng (Hong Kong University of Science and Technology)
Tulczyjew's approach for particles in gauge fields

Abstract: In this talk, we shall report that, via an idea due to Shlomo Sternberg, Tulczyjew's original approach to the dynamics of an "electrically-neutral" particle works equally well for the dynamics of an "electrically-charged" particle in non-abelian gauge fields.

Norbert Poncin (University of Luxemburg)
Multi-graded algebra and geometry

Abstract: The aim of the talk is to present a generalization of superalgebra and supergeometry to \mathbb{Z}_2^n -gradings, $n > 1$. The corresponding sign rule is not given by the product of the parities, but by the scalar product of the involved \mathbb{Z}_2^n -degrees. This \mathbb{Z}_2^n -supergeometry exhibits interesting differences with classical supergeometry, provides a sharpened viewpoint, and has better categorical properties. Further, it is closely related to Clifford calculus: Clifford algebras have numerous applications in Physics, but the use of \mathbb{Z}_2^n -gradings has never been investigated. If time permits, the \mathbb{Z}_2^n -Berezinian determinant and the corresponding integration theory will be discussed.

Olga Rossi (The University of Ostrava)
Geometry of PDEs and Hamiltonian systems

Abstract: TBA

Gennadi Sardanashvily (Moscow State University)
Noether theorems in a general setting. Reducible graded Lagrangians

Abstract: Noether theorems are formulated in a general case of reducible degenerate Grassmann-graded Lagrangian theory of even and odd variables on graded bundles. A problem is that any Euler-Lagrange operator satisfies Noether identities, which therefore must be separated into the trivial and non-trivial ones. These Noether identities can obey first-stage Noether identities, which in turn are subject to the second-stage ones, and so on. Thus, there is a hierarchy of non-trivial Noether and higher-stage Noether identities. This hierarchy is described in homology terms. If a certain homology regularity conditions holds, one can associate to a reducible degenerate Lagrangian the exact Koszul-Tate chain complex possessing the boundary operator whose nilpotentness is equivalent to all complete non-trivial Noether and higher-stage Noether identities. Since this complex is necessarily Grassmann-graded, Lagrangian theory on graded bundles is considered from the beginning, and is formulated in terms of the Grassmann-graded variational bicomplex. Its cohomology defines a first variational formula whose straightforward corollary is the first Noether theorem. Second Noether theorems associate to the above mentioned Koszul-Tate complex a certain cochain sequence whose ascent operator consists of the gauge and higher-order gauge symmetries of a Lagrangian system. If gauge symmetries are algebraically closed, this ascent operator is prolonged to the nilpotent BRST operator which brings the gauge cochain sequence into a BRST complex, and thus provides a BRST extension of an original Lagrangian system. [G.Sardanashvily, *arXiv:* 1411.2910]

Artur Sergyeyev (Silesian University in Opava)
A new class of (3+1)-dimensional integrable systems related to contact geometry

Abstract: We present a novel construction of integrable (3+1)-dimensional dispersionless systems possessing nonisospectral Lax pairs written in terms of contact vector fields. These systems can be solved using known techniques like the inverse scattering transform or the dressing method.

The construction in question solves a long-standing problem of generalization of the class of (2+1)-dimensional integrable dispersionless systems admitting nonisospectral Lax pairs involving Hamiltonian vector fields to (3+1) dimensions.

We demonstrate that plenty of (3+1)-dimensional integrable systems can be constructed in a systematic fashion using our approach, and thus integrable (3+1)-dimensional systems are much less exceptional than it appeared before.

In particular, we present a new (3+1)-dimensional dispersionless integrable system with an arbitrarily large finite number of components, which in the simplest non-trivial case yields a (3+1)-dimensional integrable generalization of the dispersionless Kadomtsev–Petviashvili equation. Please see [A.Sergyeyev, *arXiv:1401.2122*] for details.

Yunhe Sheng (School of Mathematics Jilin University)

Lie 2-algebras, homotopy Poisson manifolds and Courant algebroids

Abstract: In this talk, we study Maurer-Cartan elements on homotopy Poisson manifolds of degree n , which unify many twisted, or homotopy structures in Poisson geometry and mathematical physics, such as twisted Poisson manifolds, quasi-Poisson \mathfrak{g} -manifolds and twisted Courant algebroids. We prove that the cotangent bundle of a homotopy Poisson manifold of degree n is a symplectic NQ-manifold of degree $n + 1$. Using the fact that the dual of an n -term L_∞ -algebra is a homotopy Poisson manifold of degree $n - 1$, we obtain a Courant algebroid from a 2-term L_∞ -algebra \mathfrak{g} via the degree 2 symplectic NQ-manifold $T^*[2]\mathfrak{g}^*[1]$. Then, we derive a 2-term L_∞ -algebra from a given one. This construction could produce many interesting examples. By integrating the Lie quasi-bialgebroid associated to the Courant algebroid, we obtain a Lie-quasi-Poisson groupoid from a 2-term L_∞ -algebra, which is proposed to be the geometric structure on the dual of a Lie 2-algebra. At last, we obtain an Ikeda-Uchino algebroid from a 3-term L_∞ -algebra.

Alexandre M. Vinogradov (Levi-Civita Institute)

DCinCA, NPDEs and (Q)FT : some problems and perspectives

Abstract: TBA

Elizaveta Vishnyakova (MPI Bonn)

Flag supermanifolds: definition, properties and applications

Abstract: Yu.I. Manin introduced four series of compact complex homogeneous supermanifolds corresponding to four series of classical linear complex Lie superalgebras: the general linear Lie superalgebra $\mathfrak{gl}_{m|n}(\mathbb{C})$; the orthosymplectic Lie superalgebra $\mathfrak{osp}_{m|2n}(\mathbb{C})$ that annihilates a non-degenerate even symmetric bilinear form; the linear Lie superalgebra $\mathfrak{piosp}_{n|n}(\mathbb{C})$ that annihilates a non-degenerate odd skew-symmetric bilinear form; the linear Lie superalgebra $\mathfrak{q}_{n|n}(\mathbb{C})$ that commutes with an odd involution. These supermanifolds are called *supermanifolds of flags* in Case 1, *supermanifolds of isotropic flags* in Cases 2 and 3, and *supermanifolds of π -symmetric flags* in Case 4. As in the classical case flag supermanifolds are \mathcal{G} -homogeneous, where \mathcal{G} is one of the following supergroups: $\mathrm{GL}_{m|n}(\mathbb{C})$, $\mathrm{OSp}_{m|2n}(\mathbb{C})$, $\mathrm{PISp}_n(\mathbb{C})$ or $\mathrm{Q}_n(\mathbb{C})$, respectively.

We will give the notion of a flag supermanifold via functor of points and as a factor of a Lie supergroup modulo a parabolic subgroup. Further, we will discuss several

unexpected properties of flag supermanifolds. For example, almost all flag supermanifolds fail to possess an embedding in a projective superspace. Another interesting question here is whether a flag supermanifold has a non-trivial local deformation. If we have time we will give some applications of flag supermanifolds in representation theory of classical Lie superalgebras and in the theory of super Riemann surfaces.

Luca Vitagliano (University of Salerno)

Vector bundle valued differential forms on NQ -manifolds

Abstract: Geometric structures on NQ -manifolds, i.e. non-negatively graded manifolds with an homological vector field, encode non-graded geometric data on Lie algebroids and their higher analogues. A particularly relevant class of structures consists of vector bundle valued differential forms. (Pre-)symplectic forms, (pre-)contact structures and, more generally, distributions are in this class. I describe vector bundle valued differential forms on non-negatively graded manifolds in terms of non-graded geometric data. Moreover, I use this description to present, in a unified way, novel proofs of known results, and completely new results about degree one NQ -manifolds equipped with certain geometric structures, namely symplectic structures, contact structures, (already present in literature) and, more generally, locally conformal symplectic, presymplectic and pre-contact structures (not yet present in literature). I also discuss the case of generic vector bundle valued higher order forms, in particular multisymplectic structures.

Cornelia Vizman (West University of Timisoara)

Title: TBA

Abstract: TBA

Aissa Wade (Penn State University)

On cosymplectic groupoids

Abstract: TBA

Ping Xu (Penn State University)

Infinite jets of exponential maps and L_∞ -algebras

Abstract: Exponential maps arise naturally in the contexts of Lie theory and connections on smooth manifolds. The infinite jets of these classical exponential maps are related to the Poincaré–Birkhoff–Witt isomorphism and the complete symbol of differential operators. We will explain how to extend them to a variety of diverse situations including foliations and complex manifolds. In particular, we will show how such maps induce an interesting class of L_∞ -algebras.

POSTER SESSION

Bogdan Balcerzak (Łódz University of Technology)
Dirac operators on anchored vector bundles

Abstract: Dirac type operators on anchored vector bundles with respect to different geometric structures will be defined and discussed.

Andrew James Bruce (Polish Academy of Sciences)
Higher order mechanics on graded bundles

Abstract: We discuss the applications of the recently discovered weighted Lie algebroids to the theory of higher order Lagrangian mechanics on graded bundles following the geometric ideas of Tulczyjew. As a particular example we will focus on higher order mechanics on Lie algebroids, which is motivated by reductions of higher order systems that possess symmetries.

Ioan Bucataru (Alexandru Ioan Cuza University)
(joint work with Oana A. Constantinescu)
Generalized Helmholtz conditions for non-conservative Lagrangian systems

Abstract: In this paper we provide generalized Helmholtz conditions, in terms of a semi-basic 1-form, which characterize when a given system of second order ordinary differential equations is equivalent to the Lagrange equations, for some given arbitrary non-conservative forces. Our formulation allows, in some cases, to study the formal integrability of the proposed generalized Helmholtz conditions. These conditions, when expressed in terms of a multiplier matrix, reduce to those obtained previously by Mestdag, Sarlet and Crampin, for the particular case of dissipative or gyroscopic forces. We provide examples where the proposed generalized Helmholtz conditions, expressed in terms of a semi-basic 1-form, can be integrated and the corresponding Lagrangian and Lagrange equations can be found.

Ogul Esen (Yeditepe University)
(joint work with Hasan Gümral (Australian College of Kuwait))
Tulczyjew's triplet for Lie groups

Abstract: All semidirect products and functorial trivializations of first order and iterated bundles over a Lie group are presented. Symplectic reductions of iterated bundles by right invariance result in Tulczyjew's triplet for reduced manifolds. The trivialized Euler-Lagrange and Hamilton's equations are obtained and presented as Lagrangian submanifolds of the trivialized Tulczyjew's symplectic space. Euler-Poincaré and Lie-Poisson equations are presented as Lagrangian submanifolds of the reduced Tulczyjew's

symplectic space. Tulczyjew's generalized Legendre transformations for trivialized and reduced dynamics are constructed.

Christian Ida (Transilvania University of Brasov)

An almost contact Lie algebroid structure of the vertical Liouville distribution on the big-tangent manifold

Abstract: In this paper we introduce a natural framed $f(3, 1)$ -structure of corank 2 on the vertical bundle over the big-tangent manifold associated to a Riemannian space (M, g) . When we restrict it to an integrable vertical Liouville distribution over the big-tangent manifold, which has a natural structure of Lie algebroid, we obtain an almost contact structure.

Igor Kanatchikov (University of St Andrews)

From the polysymplectic structure to field quantization, YM mass gap and quantum gravity

Abstract: I outline the algebraic structures which can be obtained from the polysymplectic structure in field theory as generalizations of the Poisson bracket in mechanics. One of them is the Poisson-Gerstenhaber bracket of differential forms. I show how a quantization of a Heisenberg subalgebra of Poisson-Gerstenhaber algebra of forms leads to a construction of quantum fields viewed as sections of the Clifford bundle over the finite dimensional covariant configuration bundle of fields. I also outline how this reformulation of quantum field theory based on the mathematical structures of the De Donder-Weyl covariant Hamiltonian theory can be applied to the mass gap problem in quantum Yang-Mills theory and quantum gravity.

Antonio De Nicola (University of Coimbra)

Geometry and topology of cosymplectic spheres

Abstract: The notion of cosymplectic structure was introduced by P. Libermann in the late 50s as a pair (η, Ω) , where η is a closed 1-form and Ω a closed 2-form on an $2n + 1$ -dimensional manifold M , such that $\eta \wedge \Omega^n$ is a volume form. Cosymplectic manifolds play an important role in the geometric description of time-dependent mechanics (see [B. Cappelletti Montano, A. De Nicola, I. Yudin *Rev. Math. Phys.* **25** (2013), 1343002] and references therein). Starting from 1967, when Blair defined an adapted Riemannian structure on a cosymplectic manifold, a study of the metric properties on these manifolds was also initiated.

We study the geometry and topology of cosymplectic circles and cosymplectic spheres, which are the analogues in the cosymplectic setting of contact circles and contact spheres, introduced by [H. Geiges, J. Gonzalo *Invent. Math.* **121**, 147–209 (1995)], and then generalized by [M. Zessin *Ann. Inst. Fourier (Grenoble)* **55**, 1167–1194 (2005)]. We provide a complete classification of 3-dimensional compact manifolds that admit

a cosymplectic circle.

We introduce the notion of tautness and of roundness for a cosymplectic p -sphere. To any taut cosymplectic circle on a three-dimensional manifold M we are able to associate canonically a complex structure and a conformal symplectic couple on $M \times \mathbb{R}$.

In dimension three a cosymplectic circle is proved to be round if and only if it is taut. In higher dimensions we provide examples of cosymplectic circles which are taut but not round and examples of cosymplectic circles which are round but not taut. Finally we show that the three cosymplectic structures of any 3-cosymplectic manifold generate a cosymplectic sphere which is both round and taut.

Joana Nunes da Costa (University of Coimbra)
Triples of non-degenerate 2-forms on a Lie algebroid

Abstract: We show that starting with three non-degenerate 2-forms on a Lie algebroid that satisfy a simple condition, we may obtain several interesting structures.

Paul Popescu (University of Craiova)
On some classes of nonlinear constraints

Abstract: Some geometric properties of an important class of mechanical systems with nonlinear constraints are studied. A discrete version is also considered.

Yunhe Sheng (School of Mathematics Jilin University)
Graded Poisson manifolds up to homotopy

Abstract: In this paper, we introduce a notion of a graded Poisson manifold up to homotopy, namely a Poisson $[n, k]$ -manifold, motivated by studying the dual of a Lie 2-algebra. We further study Maurer-Cartan elements on Poisson $[n, k]$ -manifolds and symplectic $[n, n]$ -manifolds. There are many interesting examples such as n -term L_∞ -algebras, twisted Poisson manifolds, quasi-Poisson \mathfrak{g} -manifolds and twisted Courant algebroids. As a byproduct, we justify that the symplectic $[n, n]$ -manifold is a homotopy version of the symplectic NQ-manifold and the Maurer-Cartan equation is a homotopy version of the master equation. The dual of an n -term L_∞ -algebra is a Poisson $[n, n]$ -manifold. We prove that the cotangent bundle of a Poisson $[n, n]$ -manifold is a symplectic NQ-manifold of degree $n+1$. In particular, we construct a Courant algebroid from a 2-term L_∞ -algebra. By analyzing these structures, we obtain a Lie-quasi-Poisson groupoid from a Lie 2-algebra, which we propose to be the geometric structure on the dual of a Lie 2-algebra. At last, we obtain an Ikeda-Uchino algebroid from a 3-term L_∞ -algebra.

Alfonso Giuseppe Tortorella (University of Florence)
(joint work with Y.-G. Oh (IBS Center for Geometry and Physics), H. V. Lê (Inst. of Math. at ASCR) and L. Vitagliano (University of Salerno))
Deformations of coisotropic submanifolds in abstract Jacobi manifolds

Abstract: In this work, using the Atiyah algebroid and first order multi-differential calculus on non-trivial line bundles, we attach an L_∞ -algebra to any coisotropic submanifold S in an abstract (or Kirillov's) Jacobi manifold. Our construction generalizes and unifies analogous constructions in the symplectic case (Oh and Park), the Poisson case (Cattaneo and Felder), locally conformal symplectic case (Lê and Oh). As a new special case, we attach an L_∞ -algebra to any coisotropic submanifold in a contact manifold, including Legendrian submanifolds. The L_∞ -algebra of a coisotropic submanifold S governs the (formal) deformation problem of S .

LIST OF PARTICIPANTS

Bogdan Balcerzak	(Łodz University of Technology)
Andrew James Bruce	(Institute of Mathematics Polish Academy of Sciences)
Ioan Bucataru	(Alexandru Ioan Cuza University)
Jose-Fernando Carinena	(University of Zaragoza)
Michel Cahen	(Universite Libre de Bruxelles)
Paweł Ciosmak	(University of Warsaw)
Pantelis Damianou	(University of Cyprus)
Ogul Esen	(Yeditepe University)
Barbara Gołubowska	(Institute of Fundamental Technological Research Polish Academy of Sciences)
Katarzyna Grabowska	(University of Warsaw)
Janusz Garbowski	(Institute of Mathematics Polish Academy of Sciences)
Partha Guha	(S. N. Bose National Centre for Basic Sciences)
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Cristian Ida	(Transilvania University of Brasov)
Jacek Jezierski	(University of Warsaw)
Madeleine Jotz Lean	(University of Sheffield)
Michał Józwiowski	(Institute of Mathematics Polish Academy of Sciences)
Igor Kanatchikov	(University of St Andrews)
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Yvette Kosmann-Schwarzbach	(Ecole Polytechnique)
Vasyl Kovalchuk	(Institute of Fundamental Technological Research Polish Academy of Sciences)
Stephen Kwok	(University of Luxembourg)
Manuel de Leon	(Instituto de Ciencias Matematicas)
Konrad Lompert	(Nicolaus Copernicus University)
Javier de Lucas	(University of Warsaw)
Kirill Mackenzie	(University of Sheffield)
Franco Magri	(Universita' di Milano Bicocca)
Charles-Michel Marle	(Universite Pierre et Marie Curie)
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Miguel-C. Munoz-Lecanda	(Technical University of Catalonia)
Zoltan Muzsnay	(University of Debrecen)
Antonio de Nicola	(University of Coimbra)
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Andriy Panasyuk	(University of Warmia and Mazury)
Fani Petalidou	(Aristotle University of Thessaloniki)
Norbert Poncin	(University of Luxemburg)
Paul Popescu	(University of Craiova)
Witold Respondek	(INSA de Rouen)
Olga Rossi	(University of Ostrava)
Mikołaj Rotkiewicz	(University of Warsaw)
Ewa Eliza Rożko	(Institute of Fundamental Technological Research Polish Academy of S
Gennadi Sardanashvily	(Moscow State University)
David Saunders	(University of Ostrava)
Artur Sergyeyev	(Silesian University in Opava)
Yunhe Sheng	(School of Mathematics Jilin University)
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