

# Role of normal layer in ferromagnetic Josephson junctions

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SI<sub>1</sub>S<sub>2</sub>F<sub>1</sub>S<sub>2</sub> & передел  
тонк. слой

Using the Usadel equation approach, we have calculated the critical current density in ferromagnetic (F) Josephson junctions of different types containing insulating (I) and normal metal (N) layers in the weak link region. Even a thin additional N layer may change the boundary conditions at the SF or IF interface, where S is a superconducting electrode. We show that inserting an N layer may increase the critical current density  $J_c$  and shift the  $0-\pi$  transition to larger or smaller values of the thickness  $d_F$  of the ferromagnet, depending on the boundary parameters.

The coexistence and competition of ferromagnetic and superconducting ordering leads to a rich spectrum of unusual physical phenomena, intensively studied during the recent years [1,2]. One of the consequences is the so-called  $\pi$  Josephson junction with phase shift  $\pi$  in ground state. One or two insulating (I) barriers may be introduced at the SF interfaces as well, in order to change the product  $J_c R_N$  in the  $\pi$ -phase. Here  $J_c$  is the critical current density of the junction and  $R_N$  is its normal resistance.

nowadays, the development of magnetic memory cells and rapid single flux quantum (RSFQ) logics becomes more and more actual [3]. Only recently, a new type of magnetic memory element based on FJJs with a complex ferromagnet-superconductor-insulator weak link (FSI) was proposed [4,5]. These FJJs have a large  $J_c R_N$  product in the  $\pi$ -phase, which is required for the reliable work of such junctions in devices. The middle superconducting "s" layer is inserted in the weak link to recover the superconducting pairing and increase  $J_c$ . The thickness of this layer is of the order of the coherence length so that it may make a transition to the normal state at different conditions than the thick outer S electrodes. One of the aims of our calculation is to study the behavior of such SI<sub>1</sub>S<sub>2</sub>F<sub>1</sub>S<sub>2</sub> FJJs when their middle superconducting layer is in the normal state.

Introducing a normal metal (N) layer between the F layer and the S electrode into an FJJ is technologically necessary. Such an additional N layer was used in many FJJs. However, it was not taken into account by the theoretical explanation of these experiments. The Josephson junction we consider consists of two thick S

electrodes enclosing a thin N and an F layer (Fig.1). The N layer has a thickness  $d_N$ , while the F layer has a thickness  $d_F$ . In our model, an additional N layer at the FS interface as well as insulating layers at the SN or FS interfaces can easily be considered.

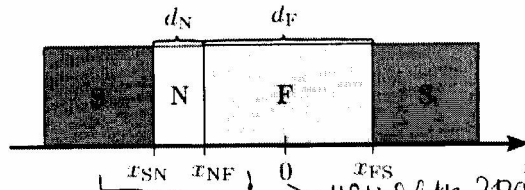


Fig 1. The sketch of one type of the considered junctions. *меняет гран. услов.*

We calculate the critical current density  $J_c$  of these configurations by determining their Green's functions in the "dirty" limit. We determine the Green's functions with the help of the Usadel equations, which we use in the theta parametrization. The Kupriyanov-Lukichev boundary conditions at all interfaces were used.

It was shown earlier [6-9] that insulating barriers decrease the critical current density and shift the  $0-\pi$  transitions to smaller values of the ferromagnet thickness  $d_F$ . A thin N layer inserted between S and I layers does not significantly influence the Josephson effect. However, if the N layer is inserted between I and F layers, it can have a large effect on the  $J_c(d_F)$  curve. If additionally the transport properties of the F and N layers differ significantly ( $\gamma_{NF} \ll 1$ ), the presence of the N layer increases the amplitude of  $J_c$  and shifts the first  $0-\pi$  transition to larger  $d_F$ , see Figs. 2(b,c,d).

The oscillation period of  $J_c(d_F)$  is still determined by the relation of the magnetic exchange energy  $H$  and the diffusion coefficient  $D_F$  in the dirty limit. If the

*нормальный слой "включает"*

Секция 1. Сверхпроводящие наносистемы

*влияет. I слой } => сдвигает точку 0-π перехода в обе стороны d\_F/ξ*

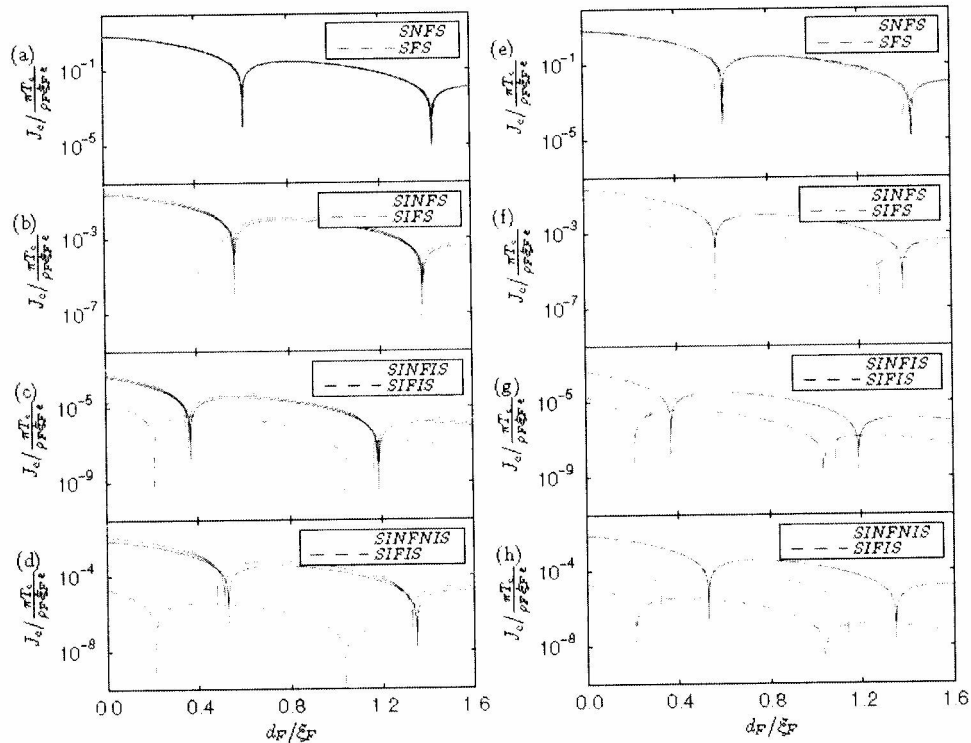
transport properties of the N layer are the same as those of the ferromagnet, the  $J_c(d_F)$  pattern does not change. This means in particular, that the dead layer plays only a role if its properties differ from the ones of the ferromagnet, not only in terms of the absence of ferromagnetism, but also in terms of its resistance. The smaller the value of  $\gamma_{NF}$ , the larger is the change of the  $J_c$  amplitude and the shift of the 0- $\pi$  transitions, see Figs.2 (f,g,h). The situation is completely different in the case of transparent SF interfaces without an I layer in between. In this case the additional thin normal layer with conductivity much larger than one of the ferromagnet ( $\gamma_{NF} \ll 1$ ) does not play any role. In the same setup, an N layer with transport properties similar to the ones of the ferromagnet ( $\gamma_{NF} \sim 1$ ) provides a decrease of the  $J_c$  amplitude and a shift of the 0- $\pi$  transition to smaller  $d_F$ , see Fig.2(e). This happens because the Josephson phase drops partially across the N layer.

Even a thin additional N layer may change the boundary conditions at the IF boundary depending on the value of  $\gamma_{NF}$ . It effectively mitigates the effect of the insulating barrier on the decaying oscillations of the critical current density  $J_c(d_F)$ . Even technological thin N lay-

ers, which almost do not suppress the superconducting correlation, have to be taken into account for the explanation of experimental results for FJJs. For example, the 0 and  $\pi$  states in FJJs proposed recently [10] for a cryogenic magnetic memory, should be determined very carefully.

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**Fig 2.** The critical current density  $J_c(d_F)$  for different FJJs. Solid lines are for the structures with different thicknesses of N layer, the dashed lines are the solutions without the N layer. In Figs. (a-d) the solid lines are getting darker as  $d_N$  becomes thicker. In Figs.2 (e-h) the solid lines are getting darker with decreasing the suppression boundary parameter  $\gamma_{NF} = 1, 0.1, 0.01$ .