

Modulation of a surface plasmon-polariton resonance by subterahertz diffracted coherent phonons

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Coherent sub-THz phonons incident on a gold grating that is deposited on a dielectric substrate undergo diffraction and thereby induce an alteration of the surface plasmon-polariton resonance. This results in efficient high-frequency modulation (up to 110 GHz) of the structure's reflectivity for visible light in the vicinity of the plasmon-polariton resonance. High modulation efficiency is achieved by designing a periodic nanostructure which provides both plasmon-polariton and phonon resonances. Our theoretical analysis shows that the dynamical alteration of the plasmon-polariton resonance is governed by modulation of the slit widths within the grating at the frequencies of higher-order phonon resonances.

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Creating new devices based on plasmonic nanostructures (PNs) requires development of new physical concepts where the properties of plasmons and their interaction with photons may be controlled externally. Several methods of this “active plasmonics”^{1,2} were reported where the energy and propagation of plasmons were controlled by temperature,³ optical excitation,^{4–7} and electric⁸ and magnetic fields.^{9–11} In order to explore the properties of plasmons in nanodevices it is necessary to realize nondestructive control of plasmons on time scales far below 1 ns. In particular, such techniques could be employed in recently developed plasmon lasers (spasers) to enhance their functionality.^{12,13} Only then the advantage of plasmonics as compared traditional integrated electronics may be indeed exploited.

By now there are a number of works where ultrafast control of plasmons in PNs has been demonstrated using femtosecond optical excitation^{14,15} which possess a number of undesirable side effects, such as thermal heating or excitation of high-energy electron states. Besides modulation of the PN dielectric function, plasmonic states may be controlled by modulation of the geometrical parameters of the PN, such as the size of elements or distances between elements. This can be realized by applying uniaxial stress^{16,17} and, for dynamical modulation, acoustic waves may be used. The feasibility of such an acoustic approach for the modulation of plasmonic properties has been already shown in a number of recent works, where THz phonons interact with the plasmon resonance in a very small noble metal particle,^{18,19} or in periodic structures but in the frequency range up to 10 GHz.^{20–22}

The aim of the present Rapid Communication is to realize an efficient modulation by sub-THz coherent phonons in a PN which has a narrow band surface-plasmon-polariton (SPP) resonance in the visible range. The main difficulty in realizing such a task lies in the fact that the typical sizes determining the PN properties at optical frequencies are much larger than the wavelength Λ of THz phonons (e.g., metal grating periods of $d = 100\text{--}1000$ nm compared to ~ 10 nm phonon wavelength). This difference results in a negligibly

small modulation efficiency. In the present work we explore the diffraction of sub-THz phonons by a plasmonic grating. For such a concept the periodic character of the PN has two roles, given by two types of resonances: one is an optical, i.e., SPP resonance, and the second one is a phonon resonance related to high-order diffraction of near-surface longitudinal acoustic phonons.

The PN used in the present experiments is a gold (Au) grating fabricated on the (111) plane of a gadolinium gallium garnet (GGG) substrate, shown in Fig. 1(a). The grating period $d = 400$ nm, thickness of Au stripes $h = 80$ nm, and width of slits $r = 50$ nm were optimized to have distinct spectral lines in the specular optical reflectivity spectra shown in Fig. 1(b), recorded for several incidence angles α with the electrical field vector lying in the incidence plane (p polarization). The spectra shown are taken for $T = 300$ K, but they don't change for $T = 5$ K. The dispersion of the spectral position of these lines versus α corresponds well to the solution of the momentum conservation law for the plasmonic wave at the GGG/Au interface:²³

$$k_0\sqrt{\varepsilon_3}\sin\alpha = \beta + m\frac{2\pi}{d}, \quad (1)$$

where k_0 is the incident light wave number, ε_1 , ε_2 , and ε_3 are the dielectric constants of gold, GGG, and air, respectively, $\beta = k_0\sqrt{\varepsilon_1 \cdot \varepsilon_2 / (\varepsilon_1 + \varepsilon_2)}$, and m is an integer. Comparison with the experimental reflection spectra indicates that the observed resonance features are due to excitation of the first-order SPPs at the GGG/Au interface, i.e., $m = 1$. Details of the optical properties of the studied PN may be found elsewhere.^{10,14}

The experimental scheme is shown in Fig. 1(c). A 50 nm Al film was deposited on the GGG substrate surface opposite to the grating. It was optically excited by femtosecond pump pulses (see the Supplemental Material²⁴ for details), which results in the injection of a bipolar strain pulse into the GGG substrate. It has an amplitude up to 10^{-3} and ~ 10 ps duration.^{25,26}

The strain pulse, which corresponds to an acoustic wave packet with sub-THz frequencies, propagates through the

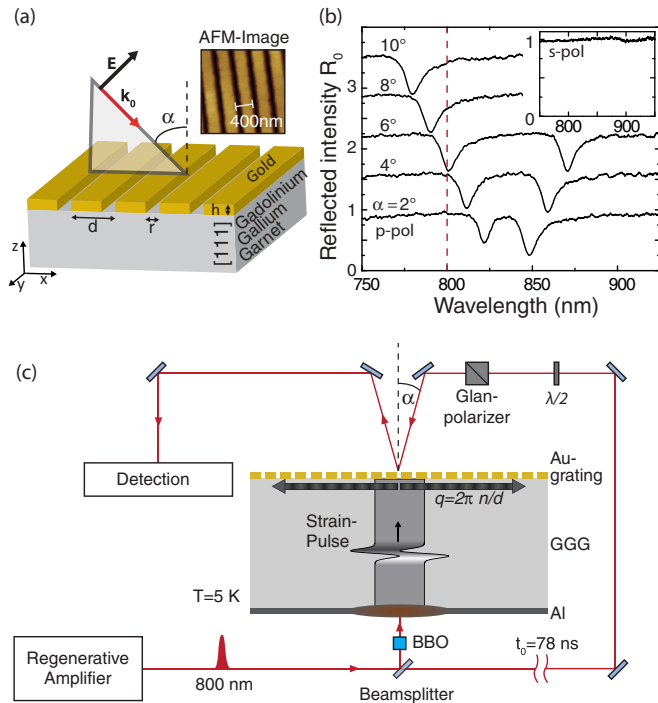


FIG. 1. (Color online) (a) The scheme of the sample and AFM image of the grating. (b) The reflectivity spectrum for p -polarized white light from the Au grating on a GGG crystal measured for several incident angles. (c) The setup of the experiments with picosecond strain pulses. The horizontal arrows at the surface with the grating show schematically diffracted acoustic waves which modulate the surface plasmon polaritons at the Au grating/GGG interface.

500 μm thick GGG substrate at the velocity of longitudinal sound 6400 m/s and reaches the grating after $t_0 = 78$ ns. There the strain pulse excites a number of elastic modes with wave vectors \mathbf{q} parallel to the surface of the grating. There are two types of excited modes which are relevant for our analysis. The first type of mode originates from pure surface acoustic waves of GGG covered by the gold film. The zone-center waves are coupled to the normal incidence bulk waves. For our structure, we estimate the frequency of such waves to be in the range of 5–7.5 GHz. Similar modes were observed in previous acousto-optical experiments.^{7,22,27} The second type of mode, shown schematically by the horizontal arrows in Fig. 1(c), has a bulk nature and propagates in GGG after diffraction from the periodic grating structure. Among these modes there are longitudinal acoustic (LA) waves propagating in the bulk of GGG with \mathbf{q} parallel to the surface of the grating and perpendicular to the Au stripes, i.e., $\mathbf{q} \parallel \mathbf{x}$. These near-surface modes exhibit the properties of bulk LA waves in GGG and govern the most interesting observations in the present work.

Modes of both types (i.e., surface and near-surface modes) propagate along the Au grating/GGG interface and induce coherent displacements of the grating elements, thereby modulating its geometric parameters. Such modulation is detected by monitoring the intensity I of a reflected optical probe pulse with 800 nm wavelength (see the Supplemental Material²⁴ for details).

We performed experiments at cryogenic temperatures ($T = 5$ K) where the attenuation of sub-THz LA waves during their

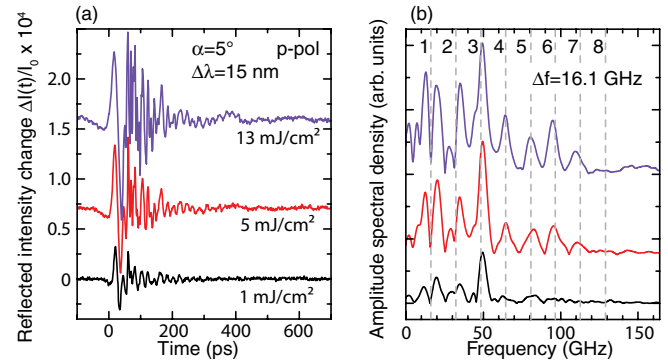


FIG. 2. (Color online) (a) The temporal evolutions of the reflected intensity changes induced by the picosecond strain pulse measured for three pump excitation densities W . The probing spectral width was $\Delta\lambda = 15$ nm and the incident angle $\alpha = 5^\circ$. (b) The amplitude fast Fourier transforms of the corresponding temporal traces shown in (a). The vertical dashed lines indicate the frequencies expected for the acoustic modes diffracted by the Au grating and propagating parallel to surface in the GGG substrate [see Eq. (2)]. The integers at the top of the panel indicate the diffraction order n . $T = 5$ K.

propagation through the GGG substrate can be neglected.²⁸ The results are shown in Fig. 2. Figure 2(a) shows the temporal evolutions of the intensity changes $\Delta I(t)/I_0 = [I(t) - I_0]/I_0$ for three pump excitation densities W (t is the time between the arrival of the strain pulse at the GGG/Au grating interface and the probe pulse, and I_0 is the stationary intensity of the reflected probe beam without the strain pulse). Complicated oscillatory behaviors of $\Delta I(t)/I_0$ are observed in all three curves. The exact evolution of $\Delta I(t)/I_0$ depends on W . In particular, the changes in reflectivity start earlier for high W , which is in agreement with the appearance of nonlinear phenomena during strain pulse propagation for $W > 1$ mJ/cm^2 .²⁹ The absolute changes of the reflected intensity reach 2×10^{-4} for the highest W [$\sim 10^{-6}$ (Ref. 21) to $\sim 10^{-3}$ (Ref. 7) in comparable works] and depend also on the incidence angle and polarization of the probe beam. The curves in Fig. 2(a) are obtained for p -polarized light at $\alpha = 5^\circ$ when the central wavelength of the probe beam lies at 800 nm, i.e., on the short-wavelength flank of the SPP resonance [see Fig. 1(b)]. The signal is zero for probing by s -polarized light (electric field perpendicular to the incidence plane) for which no SPP peaks are observed at any α , due to the boundary conditions [Fig. 1(b) inset and Fig. S2(a) in the Supplemental Material²⁴]. Also, $\Delta I(t)/I_0 = 0$ for both polarizations for $\alpha = 2^\circ$, because in this case the spectral overlap between the polariton and the probe spectral lines is negligible (Fig. S3 in the Supplemental Material²⁴). Thus we may conclude that the observed signal $\Delta I(t)/I_0$ is exclusively resulting from modulation of the SPP resonance by the elastic waves excited by the picosecond strain pulse.

The amplitude spectra of the modulation signals, obtained by fast Fourier transformation of the measured $\Delta I(t)/I_0$, are shown in Fig. 2(b) for the same W as in Fig. 2(a). For the highest W [top curve in Fig. 2(b)] the spectrum spreads up to $f = 110$ GHz. The spectrum consists of a number of peaks whose frequencies do not depend on W . For lower W , on

the other hand, the high-frequency peaks are less pronounced compared to high W values.

The remarkable result of Fig. 2(b) is the observation of an almost equidistant spectral separation between the spectral lines for $f > 30$ GHz. The central frequencies of these spectral lines are well described by

$$f_n = \frac{ns}{d}, \quad (2)$$

where n is an integer and $s = 6440$ m/s is close to the LA velocity for waves propagating in GGG along the (111) plane.³⁰ The appropriateness of describing the modulation frequencies by Eq. (2) leads us to the explanation that the components in the modulation spectrum are governed by the LA near-surface waves, which are diffracted by the grating and propagate in GGG with the sound velocity s along the x direction. The integer n corresponds to the interference order of the diffracted waves. In other words, the Au grating plays the role of a diffraction grating for acoustic waves in addition to the SPP-photon coupling that it provides. The diffracted acoustic waves propagating along the GGG/grating interface initiate the sub-THz modulation of the reflected light intensity in the spectral region of the SPP resonance. The intensity excess of the 49 GHz peak ($n = 3$) relative to the other peaks in Fig. 2(b) is likely due to the maximum at 20–80 GHz in the spectrum of the incident strain pulse.²⁵ The spectral lines which would correspond to transverse acoustic (TA) phonons are not observed experimentally. If they were present, they would be easily recognized due to the smaller TA sound velocity. We attribute the absence of TA peaks to the mechanical boundary conditions which control the transformation of the incident LA strain pulse into diffracted TA waves. It is worth mentioning that the bulk to surface transformation of low-frequency acoustic waves was shown earlier.^{31,32}

The widths of the spectral lines are almost independent on n up to $n = 7$. Such behavior is similar to optical diffraction on gratings where the spectral width for a certain angle does not depend on the diffraction order but is governed by the number N of coherently interfering grating periods.³³ From the experimental data, we estimate $N \approx 3$ for the number of “active” grating periods, corresponding to a lateral size of more than $1 \mu\text{m}$.

The experimental results show that the detection mechanism is governed by the SPP resonance. As already mentioned, the modulation of the reflected intensity I is observed only when SPPs are excited. For excitation with s polarization or incident angle out of the SPP resonance there is no modulation observed (Figs. S2 and S3 in the Supplemental Material²⁴). Below we present the theoretical analysis of the coupling between the SPPs and the near-surface acoustic waves, which governs the measured optical response at high frequencies ($f > 30$ GHz). The elasticity equations show that the lateral displacement profile is an odd function of x with respect to the middle of the grating stripes,³⁴ provided that the grating profile is an even function of x . Therefore, we may assume that the main contribution to $\Delta I(t)/I_0$ comes from the coherent modulation of the slit width r , while the period d of the grating remains unperturbed. Variation of r acts on the PN in two ways: (i) It modifies the coupling of the two SPPs

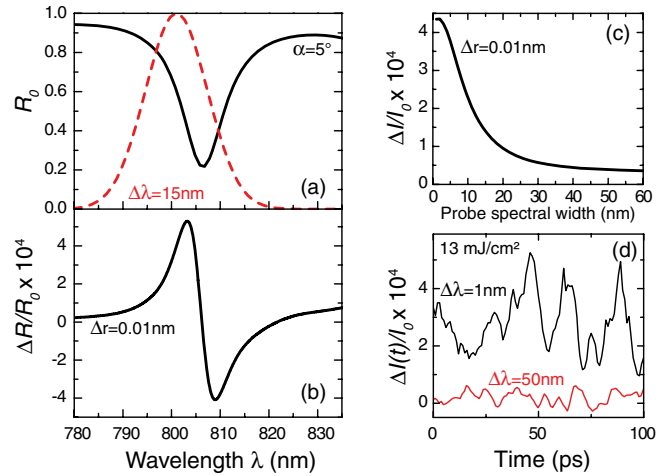


FIG. 3. (Color online) (a) The calculated reflectivity spectrum (solid line) and spectrum of the probe pulse with the spectral width $\Delta\lambda = 15$ nm (dashed line). (b) The calculated differential spectrum $\Delta R/R_0$ when the width of the slit in the Au grating changes by $\Delta r = 0.01$ nm. (c) The calculated dependence of the relative reflected intensity changes for a probe pulse centered at 800 nm on the spectral width $\Delta\lambda$. (d) The measured 100 ps fragments of the reflectivity signals for probing with $\Delta\lambda = 1$ nm (upper curve) and $\Delta\lambda = 50$ nm (lower curve). In all curves the central wavelength of the probing beam was $\lambda = 800$ nm, the incident angle was $\alpha = 5^\circ$, and the temperature was $T = 5$ K.

related to the gold-air and gold-GGG interface, respectively, and (ii) it perturbs the coupling strength of the incident light to the SPP. The consequences for the reflectivity spectrum are (i) the energy of the resonance is shifted, and (ii) the depth of the intensity dip at the resonance is changed. Quantitatively, both of these effects can be calculated using a rigorous coupled wave analysis (RCWA).^{35,36}

The calculated, unperturbed reflectivity spectrum R_0 for $\alpha = 5^\circ$ along with the probe spectrum is shown in Fig. 3(a). At $\alpha = 5^\circ$ the probe central wavelength is on the shorter-wavelength wing of the R_0 spectrum. The RCWA modeling shows that small changes Δr of the slit width cause a shift of the SPP resonance in the reflectivity spectrum. That is why the change of the reflectivity spectrum $\Delta R(\lambda)/R_0(\lambda) = [R(\lambda) - R_0(\lambda)]/R_0(\lambda)$ has positive and negative peaks corresponding to the wings of the plasmonic spectral line in reflection. A calculated spectrum $\Delta R/R_0$ for $\Delta r = 0.01$ nm is shown in Fig. 3(b). The measured signal $\Delta I/I_0$ integrated over the probe spectral width is sensitive to the spectral bandwidth of the probe pulse $\Delta\lambda$ [Fig. 3(c)]. The largest signal is expected for the case when the probe spectrum overlaps with the positive or negative parts of the $\Delta R/R_0$ spectrum only. This implies that there is some optimal incidence angle at which the central wavelength of the probe is located on the spectral wing of the SPP resonance and $\Delta\lambda$ is such that only one peak of $\Delta R/R_0$ acts.

The experimentally measured amplitude $\Delta I/I_0 \sim 10^{-4}$ is in good agreement with theoretical calculations, if we assume the lateral displacement to have a magnitude of $\Delta r = 0.01$ nm, resulting in a corresponding change of the slit width. For $n = 7$, this number corresponds to strain of about 10^{-3} . Taking into account that the amplitude of strain in the incident pulse

and its spectral width are $\sim 10^{-3}$ and 100 GHz, respectively, we may conclude that the grating gives rise to considerable local enhancement of the acoustic field in the relatively narrow spectral bands near f_n .

In order to confirm the calculated dependence of the modulation amplitude on $\Delta\lambda$ shown in Fig. 3(c) we have performed experiments with three different values of $\Delta\lambda$. The experimental results shown in Fig. 2 are obtained for $\Delta\lambda = 15$ nm. The signals measured for $\Delta\lambda = 1$ and 50 nm are presented in Fig. 3(d). The amplitudes of high-frequency oscillations are five times higher for $\Delta\lambda = 1$ nm than for $\Delta\lambda = 50$ nm. This is in reasonable agreement with theory predicting an order of magnitude difference. This agreement supports our assumption that the coherent modulation of the slit widths is the main mechanism for coupling the SPPs with the LA near-surface acoustic waves.

Now we turn to discussing the low-frequency ($f < 30$ GHz) part of the modulation spectrum, which consists of a series of spectral lines with central frequencies not described by Eq. (2) [see Fig. 2(b)]. For instance, the spectrum has a dip at $f = 16.1$ GHz instead of the expected peak related to the fundamental ($n = 1$) LA near-surface mode. We attribute the spectral lines in the spectral region $f < 30$ GHz to various surface modes excited in the Au grating as observed also in earlier works.^{7,22,27} The exact spectrum of the modulated signals depends on the dispersion of these modes and their interaction with bulk modes in GGG. For instance, the dip at $f = 16.1$ GHz may be due to a Fano resonance originating from the interaction of the surface modes in the Au grating and LA near-surface modes in GGG.

We also performed experiments at a temperature of 300 K when low-frequency components are fully dominant, because high-frequency oscillations in $\Delta I(t)/I_0$ are damped completely.²⁸ The results are presented in Fig. 4. The signals do not depend on $\Delta\lambda$, which means that the interaction mechanism for the low-frequency modes with the polariton resonance is different from the one described above for $f > 30$ GHz, where the modulation of the grating slit width is considered as the main perturbation. A comprehensive analysis of the surface modes is beyond the scope of the present Rapid Communication where we concentrate mostly on the high-frequency part of the modulation spectrum.

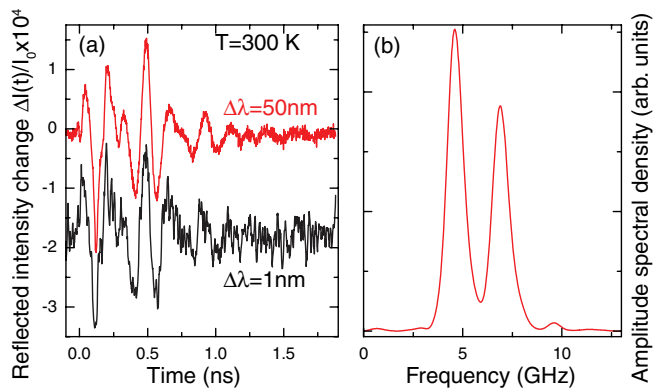


FIG. 4. (Color online) (a) The time evolution of the reflected intensity at room temperature for $\Delta\lambda = 50$ nm (upper curve) and $\Delta\lambda = 1$ nm (lower curve) ($\lambda = 800$ nm, $\alpha = 5^\circ$, and $W \sim 10$ mJ/cm²). (b) Corresponding fast Fourier transform for $\Delta\lambda = 50$ nm.

In conclusion, we have demonstrated that coherent phonons are diffracted by the plasmonic grating and this results in efficient modulation of a SPP resonance at frequencies ~ 100 GHz. The studied object is good for realizing high-frequency modulation of reflectivity due to the optical and elastic mismatch of the Au grating and GGG substrate. Such a combination is ideal for more complex sub-THz acoustic experiments in systems with waveguiding layers and magnetic films.¹⁰ The reported work provides a basic concept of exploiting the diffraction of coherent phonons, thus opening a field for applying similar principles for practical use in plasmonic devices. Further selection of the modulation frequencies may be achieved by tailoring the spectral components of the incident strain pulse, e.g., by using superlattices as transducers.³⁷

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